

# Kinematics Worksheet 1

$$\textcircled{1} \quad v = \frac{\Delta l}{\Delta t} = \frac{20}{2.35} = \underline{12.8 \text{ m/s}}$$

$$\textcircled{2} \quad v = \frac{\Delta d}{\Delta t} = \frac{280 \text{ km}}{3 \text{ h}} = 93 \text{ km/h}$$

$$\textcircled{3} \quad v_i = 0 \quad v_f = v_i + at$$
$$v_f = 27 \text{ m/s} \quad a = \frac{v_f}{t} = \frac{27}{3} = \underline{9.0 \text{ m/s}^2}$$
$$t = 3 \text{ s}$$

$$\textcircled{4} \quad v_i = 0 \quad v_f = v_i + at$$
$$a = 190 \text{ m/s}^2 \quad = 190(2.4) = \underline{456 \text{ m/s}}$$
$$t = 2.4 \text{ s}$$
$$v_f = ?$$

$$\textcircled{5} \quad v_i = 15 \text{ m/s} \quad v_f = v_i + at$$
$$a = 3.5 \text{ m/s}^2 \quad = 15 + (3.5)(5)$$
$$t = 5.0 \text{ s} \quad = \underline{32.5 \text{ m/s}}$$
$$v_f = ?$$

$$\textcircled{6} \quad v_i = 23 \text{ m/s} \quad v_f^2 = v_i^2 + 2ad$$
$$a = -0.25 \text{ m/s}^2 \quad d = \frac{-v_i^2}{2a} = \frac{-(23)^2}{2(-.25)} = \underline{1058 \text{ m}}$$
$$v_f = 0$$
$$d = ?$$

$$\textcircled{7} \quad v_i = 12 \text{ m/s} \quad d = \left(\frac{v_i + v_f}{2}\right)t$$
$$v_f = 26 \text{ m/s} \quad = \left(\frac{12 + 26}{2}\right)14 = \underline{266 \text{ m}}$$
$$t = 14 \text{ s}$$
$$d = ?$$

$$\textcircled{8} \quad v_i = 0$$

$$a = 3.2 \text{ m/s}^2$$

$$t = 3.0 \text{ s}$$

$$\begin{aligned} \text{(a)} \quad v_f &= v_i + at \\ &= 0 + (3.2 \text{ m/s}^2)(3.0 \text{ s}) \\ &= \underline{9.6 \text{ m/s}} \end{aligned}$$

$$\begin{aligned} \text{(c)} \quad d &= \left( \frac{v_i + v_f}{2} \right) t \\ &= \left( \frac{0 + 9.6 \text{ m/s}}{2} \right) (3.0 \text{ s}) \\ &= \underline{14.4 \text{ m}} \end{aligned}$$

$$\text{(b)} \quad v_{\text{avg}} = \frac{\Delta d}{\Delta t} = \frac{14.4 \text{ m}}{3.0 \text{ s}} = \underline{4.8 \text{ m/s}}$$

$$\textcircled{9} \quad v_i = 12 \text{ m/s}$$

$$v_f = 0$$

$$d = 541 \text{ m}$$

$$a = ?$$

$$d = \left( \frac{v_i + v_f}{2} \right) t$$

$$541 \text{ m} = \left( \frac{12 \text{ m/s} + 0}{2} \right) t$$

$$t = 90.17 \text{ s}$$

$$v_f = v_i + at$$

$$0 = 12 \text{ m/s} + a(90.17 \text{ s})$$

$$a = \underline{-0.13 \text{ m/s}^2}$$

$$\textcircled{10} \quad v_f = 0$$

$$a = -9.4 \text{ m/s}^2$$

$$d = 34 \text{ m}$$

$$v_i = ?$$

$$d = \left( \frac{v_i + v_f}{2} \right) t$$

$$34 = \left( \frac{v_i + 0}{2} \right) t$$

$$68 = v_i t$$

$$\frac{68}{v_i} = t$$

$$v_f = v_i + at$$

$$0 = v_i + (-9.4)t$$

$$0 = v_i + -9.4 \left( \frac{68}{v_i} \right)$$

$$v_i^2 = \frac{639.2}{v_i}$$

$$v_i^2 = 639.2$$

$$v_i = \underline{25.3 \text{ m/s}}$$

$$\begin{aligned} \textcircled{11} \quad v_i &= 0 \\ v_f &= 25 \text{ m/s} \\ a &= 0.15 \text{ m/s}^2 \\ d &=? \end{aligned}$$

$$\begin{aligned} v_f &= v_i + at \\ 25 \text{ m/s} &= 0 + (0.15 \text{ m/s}^2)t \\ t &= 166.67 \text{ s} \end{aligned}$$

$$\begin{aligned} d &= \left( \frac{v_i + v_f}{2} \right) t \\ &= \left( \frac{0 + 25 \text{ m/s}}{2} \right) 166.67 \text{ s} \end{aligned}$$

$$\underline{d = 2083 \text{ m}}$$

$$\begin{aligned} \textcircled{12} \quad v_f &= 53 \text{ m/s} \\ d &= 120 \text{ m} \end{aligned}$$

$$\begin{aligned} \text{(a)} \quad v_i &= 0 \quad d = \left( \frac{v_i + v_f}{2} \right) t \\ 120 \text{ m} &= \left( \frac{0 + 53 \text{ m/s}}{2} \right) t \\ t &= 4.53 \text{ s} \end{aligned}$$

$$\begin{aligned} v_f &= v_i + at \\ 53 \text{ m/s} &= 0 + a(4.53 \text{ s}) \\ a &= \underline{11.7 \text{ m/s}^2} \end{aligned}$$

(b) using acceleration from (a)

$$\begin{aligned} v_f &= v_i + at \\ 85 \text{ m/s} &= 0 + (11.7 \text{ m/s}^2)t \\ t &= 7.26 \text{ s} \end{aligned}$$

$$\begin{aligned} d &= \left( \frac{v_i + v_f}{2} \right) t \\ &= \left( \frac{0 + 85 \text{ m/s}}{2} \right) 7.26 \text{ s} \\ &= \underline{308 \text{ m}} \end{aligned}$$

$$\textcircled{13} \quad v = \frac{\Delta d}{\Delta t}$$

$$8.3 \text{ min}(60) = 498 \text{ s}$$

$$3 \times 10^8 \text{ m/s} = \frac{\Delta d}{498 \text{ s}}$$

$$\underline{\Delta d = 1.5 \times 10^{11} \text{ m}}$$

$$(14) v_i = 55 \text{ km/h} \left( \frac{1000 \text{ m/km}}{3600 \text{ s/hr}} \right) = 15.278 \text{ m/s}$$

Constant velocity

$$v = \frac{\Delta d}{\Delta t}$$

$$15.278 \text{ m/s} = \frac{\Delta d}{0.75}$$

$$\Delta d = \underline{11.5 \text{ m}}$$

$$(15) a = -3.0 \times 10^2 \text{ m/s}^2$$

$$v_i = 110 \text{ km/h} = 30.56 \text{ m/s}$$

$$v_f = 0$$

$$d = ?$$

$$v_f = v_i + at$$

$$0 = (30.56 \text{ m/s}) + (-3.0 \times 10^2 \text{ m/s}^2)t$$

$$t = -0.102 \text{ s}$$

$$d = \left( \frac{v_i + v_f}{2} \right) t$$

$$= \left( \frac{(30.56 \text{ m/s}) + 0}{2} \right) (0.102 \text{ s})$$

$$\underline{d = 1.6 \text{ m}}$$

(16)

$$v_i = 15 \text{ m/s}$$

$$v_f = 25 \text{ m/s}$$

$$d = 125 \text{ m}$$

$$t = ?$$

$$d = \left( \frac{v_i + v_f}{2} \right) t$$

$$t = \frac{2d}{v_i + v_f} = \frac{2(125)}{15 + 25} = 6.25 = \underline{6.3 \text{ s}}$$

(17)

(a)  $v_i = 2 \text{ m/s}$

$$a = -0.5 \text{ m/s}^2$$

$$t = 2.0 \text{ s}$$

$$v_f = ?$$

$$v_f = v_i + at$$

$$= 2 + (-0.5)(2)$$

$$= \underline{1.0 \text{ m/s}}$$

(b)

$$v_f = v_i + at$$

$$= 2 + (-0.5)(6)$$

$$= \underline{-1.0 \text{ m/s}}$$

(This means that it will stop and start to roll back down the hill.)

(18)

$$v_i = 0$$

$$a = 5.0 \text{ m/s}^2$$

$$d = 5 \times 10^2 \text{ m}$$

$$v_f = ?$$

$$v_f^2 = v_i^2 + 2ad$$

$$v_f = \sqrt{2ad}$$

$$= \sqrt{2(5)(5 \times 10^2)}$$

$$v_f = \underline{100 \text{ m/s}}$$

$$(19) \text{ (a)} \quad v_i = 6 \text{ m/s}$$

$$v_f = 0$$

$$t = 1.2 \text{ s}$$

$$d = ?$$

$$d = \left( \frac{v_i + v_f}{2} \right) t$$

$$= \frac{v_i t}{2} = \frac{6(1.2)}{2} = \underline{3.6 \text{ m}}$$

(b)

$$v_f = v_i + at$$

$$a = \frac{v_f - v_i}{t} = \frac{-v_i}{t} = \frac{-6}{1.2} = \underline{-5 \text{ m/s}^2}$$

(20)

$$v_i = 0$$

$$v_f = 61 \text{ m/s}$$

$$a = 2.5 \text{ m/s}^2$$

$$d = 1820 \text{ m}$$

$$t = ?$$

$$v_f = v_i + at$$

$$t = \frac{v_f}{a} = \frac{61}{2.5} = \underline{24 \text{ s}}$$

(21)

$$v_i = 22 \text{ m/s}$$

$$v_f = 3.0 \text{ m/s}$$

$$a = -2.1 \text{ m/s}^2$$

$$t = ?$$

$$v_f = v_i + at$$

$$t = \frac{v_f - v_i}{a}$$

$$= \frac{3 - 22}{-2.1}$$

$$\underline{t = 9.0 \text{ s}}$$

(22) (a)  $v_i = 0$   $d = v_i t + \frac{1}{2} a t^2$   
 $a = 3.0 \text{ m/s}^2$   
 $t = 30 \text{ s}$   $d = \frac{1}{2} a t^2$   
 $d = ?$   $= \frac{1}{2} (3)(30)^2 = \underline{1350 \text{ m}}$

(b)  $v_f = v_i + a t$   
 $v_f = (3)(30) = \underline{90 \text{ m/s}}$

(23) (a)  $v_i = 11.4 \text{ m/s}$   $v_f^2 = v_i^2 + 2 a d$   
 $a = -3.8 \text{ m/s}^2$   
 $v_f = 0$   $d = \frac{-v_i^2}{2a} = \frac{-(11.4)^2}{2(-3.8)} = 17.1$   
 $d = ?$

The vehicle stops in 17.1 m so the ranger comes within  $20 - 17.1 = \underline{2.9 \text{ m}}$  of the deer.

(b)  $t = ?$   
 $v_f = v_i + a t$   
 $t = \frac{-v_i}{a} = \frac{-11.4}{-3.8} = \underline{3.0 \text{ s}}$

24 (a)

Friend (A)

$$v = 3.5 \text{ m/s}$$

$$a = 0$$

Bicyclist (B)

$$v_i = 0$$

$$a = 2.4 \text{ m/s}^2$$

She catches her friend when they are both at the same place ( $d$  is equal) at the same time ( $t$  is equal)

$$d_A = v_A t_A + \frac{1}{2} a_A t_A^2$$

$$d_B = v_B t + \frac{1}{2} a_B t^2$$

$$v_A t = \frac{1}{2} a_B t^2$$

$$t = \frac{2v_A}{a_B} = \frac{2(3.5)}{2.4} = 2.92 \text{ s}$$

But, she waited 2 seconds before starting. Therefore it takes her 4.92 s to catch her friend.

$$\begin{aligned} (b) \quad d_B &= \frac{1}{2} a_B t_B^2 \\ &= \frac{1}{2} (2.4) (2.92)^2 \\ &= \underline{10.2 \text{ m}} \end{aligned}$$

\* note, she only cycled for 2.92 seconds.

$$\begin{aligned} (c) \quad v_f &= v_i + at \\ &= (2.4) (2.92) \\ &= \underline{7.0 \text{ m/s}} \end{aligned}$$